

# Calculation Policy

## Dorchester Primary School

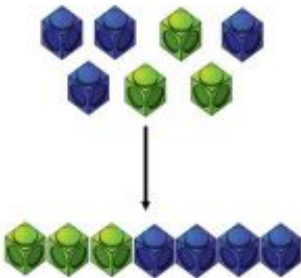
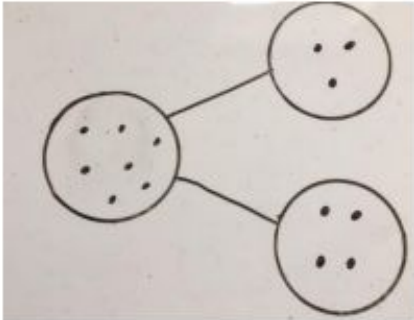
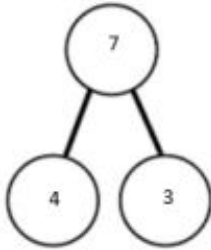

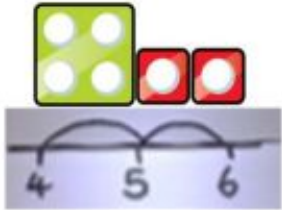
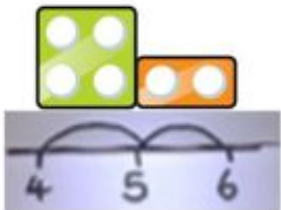
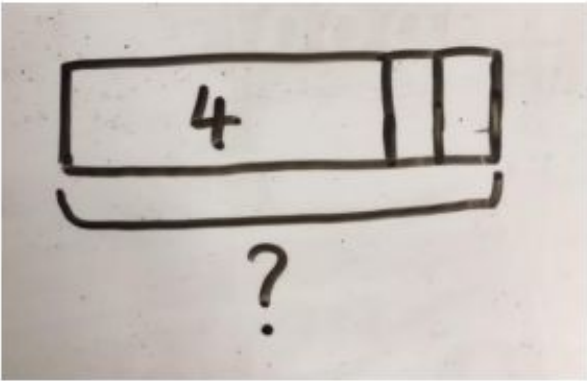



Written: April 2023  
Review April 2026

	<u>Year 1</u>	<u>Year 2</u>	<u>Year 3</u>	<u>Year 4</u>	<u>Year 5</u>	<u>Year 6</u>
<u>Addition</u>	Combining two parts to make a whole (part-part-whole model). Starting at the bigger number and counting on. Regrouping to make 10.	Adding three single digits. Expanded column method (no regrouping).	Column method with regrouping (up to 3 digits).	Column method with regrouping (up to 4 digits).	Column method with regrouping (with more than 4 digits including decimals).	Column method with regrouping (with more than 4 digits including decimals).
<u>Subtraction</u>	Taking away ones. Counting back. Finding the difference. Making 10.	Counting back. Finding the difference. Making 10. Partitioning smallest number to subtract.	Column method with regrouping (up to 3 digits).	Column method with regrouping (up to 4 digits)	Column method with regrouping (with more than 4 digits including decimals)	Column method with regrouping (with more than 4 digits including decimals)
<u>Multiplication</u>	Doubling. Counting in multiples of 2, 5 and 10. Arrays (with support.)	Doubling. Counting in multiples of 2, 3, 5 and 10. Repeated addition. Arrays showing commutative law.	Counting in multiples of 2, 3, 4, 5, 8 and 10. Repeated addition. Arrays. Grid method.	Column multiplication (2 and 3 digit x 1 digit)	Column multiplication (up to 4 digit x 1 or 2 digits)	Column multiplication (multi-digit up to 4 digits by 2 digits)
<u>Division</u>	Sharing objects into groups. Division as grouping.	Division as grouping. Division as arrays.	Division with arrays. Division with a remainder. Short division (using concrete and pictorial).	Division with arrays Division with a remainder. Short division (up to 3 digits by 1).	Short division (up to 4 digits by 1 digit – use remainders in context).	Short Division Long division (up to 4 digits by 2 digits – interpret remainders as number, fraction, decimals or rounding).

# Calculation policy: Addition

Key language: sum, total, parts and wholes, plus, add, altogether, more, 'is equal to' 'is the same as'.

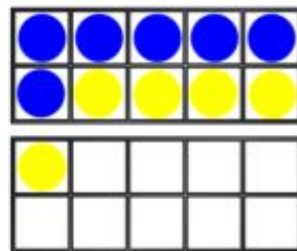
Concrete	Pictorial	Abstract
<p><b>Combining two parts to make a whole</b> (use other resources too e.g. eggs, shells, teddy bears, cars).</p> 	<p>Children to represent the cubes using dots or crosses. They could put each part on a part whole model too.</p> 	<p><math>4 + 3 = 7</math> Four is a part, 3 is a part and the whole is seven.</p> 
<p><b>Counting on using number lines</b> using cubes or Numicon.</p>   	<p>A bar model which encourages the children to count on, rather than count all.</p> 	<p>The abstract number line: What is 2 more than 4? What is the sum of 2 and 4? What is the total of 4 and 2? <math>4 + 2</math></p> 

**Regrouping to make 10;** using ten frames and counters/cubes or using Numicon.

$$6 + 5$$



Children to draw the ten frame and counters/cubes.



Children to develop an understanding of equality e.g.

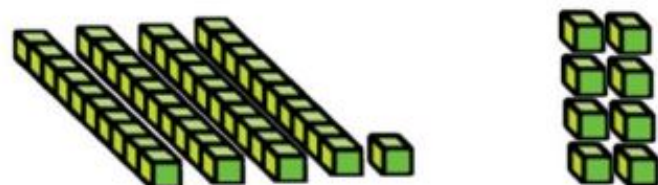
$$6 + \square = 11$$

$$6 + 5 = 5 + \square$$

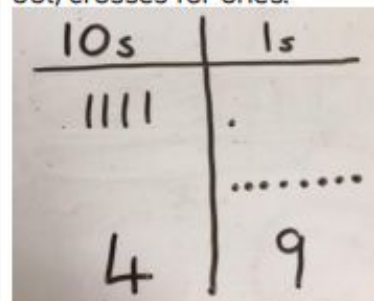
$$6 + 5 = \square + 4$$

**TO + O using base 10.** Continue to develop understanding of partitioning and place value.

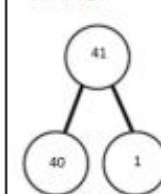
$$41 + 8$$



Children to represent the base 10 e.g. lines for tens and dot/crosses for ones.

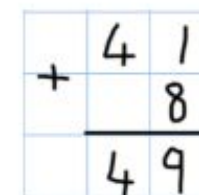


$$41 + 8$$



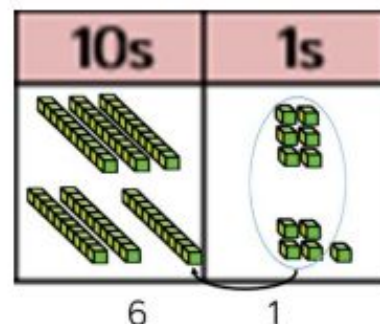
$$1 + 8 = 9$$

$$40 + 9 = 49$$

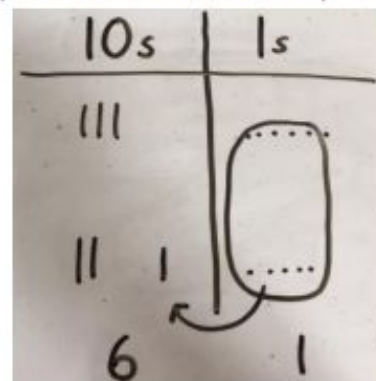


**TO + TO using base 10.** Continue to develop understanding of partitioning and place value.

$$36 + 25$$



Children to represent the base 10 in a place value chart.



Looking for ways to make 10.

$$36 + 25 =$$

$$30 + 20 = 50$$

$$5 + 5 = 10$$

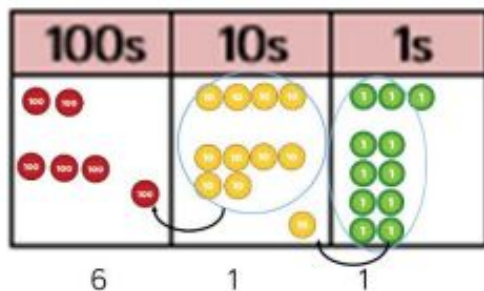
$$50 + 10 + 1 = 61$$

Formal method:

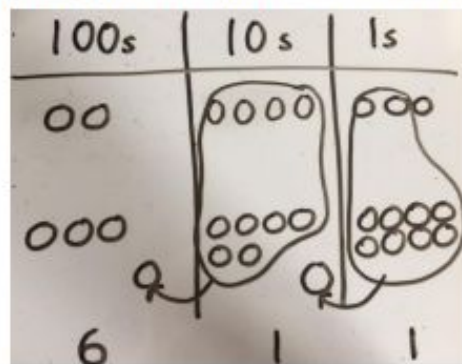
$$\begin{array}{r} 36 \\ +25 \\ \hline 61 \\ \hline 1 \end{array}$$



**Use of place value counters to add HTO + TO, HTO + HTO etc.** When there are 10 ones in the 1s column- we exchange for 1 ten, when there are 10 tens in the 10s column- we exchange for 1 hundred.



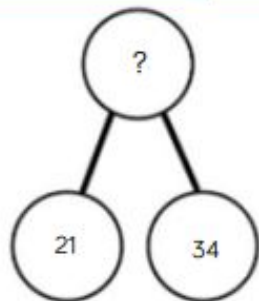
Children to represent the counters in a place value chart, circling when they make an exchange.



243

$$\begin{array}{r} 243 \\ +368 \\ \hline 611 \\ \hline 1 \quad 1 \end{array}$$

## Conceptual variation; different ways to ask children to solve $21 + 34$



?	
21	34

Word problems:

In year 3, there are 21 children and in year 4, there are 34 children. How many children in total?

$21 + 34 = 55$ . Prove it

21

+34

$21 + 34 =$

   =  $21 + 34$

Calculate the sum of twenty-one and thirty-four.

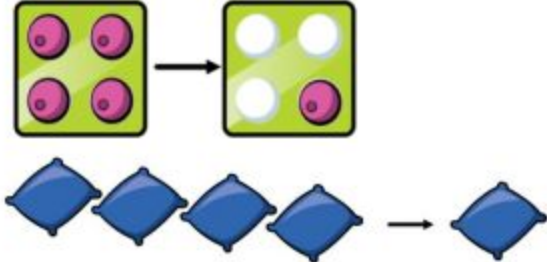
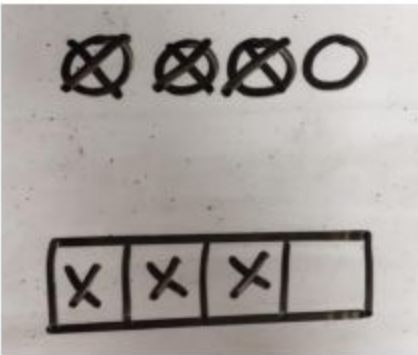

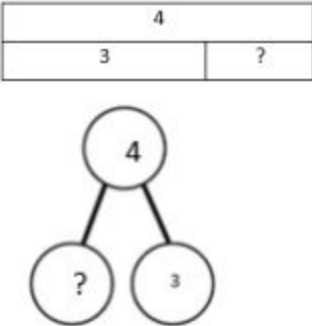

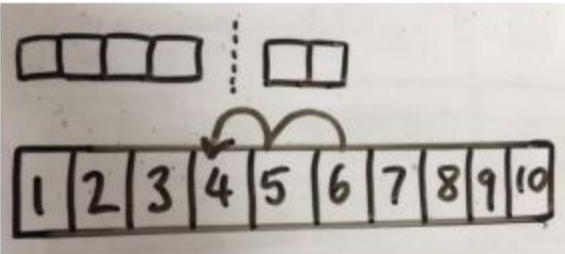
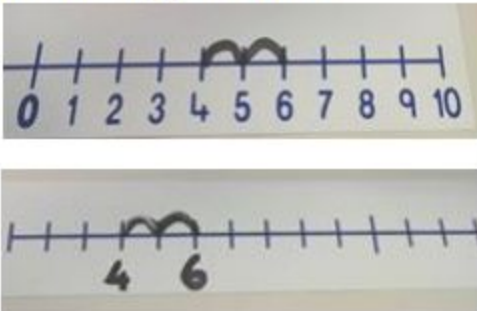


Missing digit problems:

10s	1s
20	1
30	?
?	5

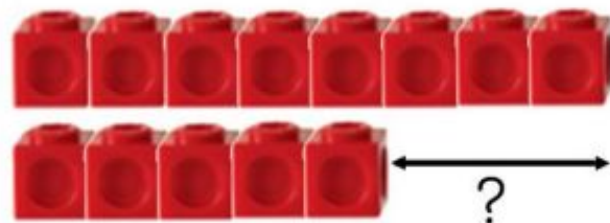
# Calculation policy: Subtraction

Key language: take away, less than, the difference, subtract, minus, fewer, decrease.

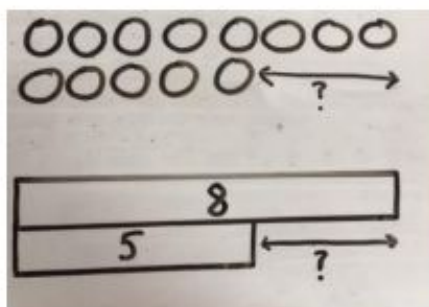
Concrete	Pictorial	Abstract
<p><b>Physically taking away and removing objects from a whole</b> (ten frames, Numicon, cubes and other items such as beanbags could be used).</p> <p><math>4 - 3 = 1</math></p> 	<p>Children to draw the concrete resources they are using and cross out the correct amount. The bar model can also be used.</p> 	<p><math>4 - 3 =</math></p> <p> <math>= 4 - 3</math></p> 
<p><b>Counting back</b> (using number lines or number tracks) children start with 6 and count back 2.</p> <p><math>6 - 2 = 4</math></p> 	<p>Children to represent what they see pictorially e.g.</p> 	<p>Children to represent the calculation on a number line or number track and show their jumps. Encourage children to use an empty number line</p> 

**Finding the difference** (using cubes, Numicon or Cuisenaire rods, other objects can also be used).

Calculate the difference between 8 and 5.



Children to draw the cubes/other concrete objects which they have used or use the bar model to illustrate what they need to calculate.



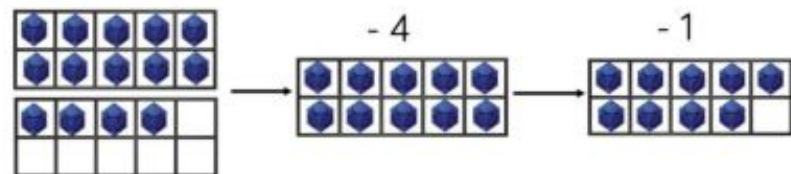
Find the difference between 8 and 5.

8 - 5, the difference is

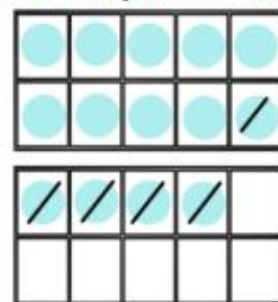
Children to explore why  
 $9 - 6 = 8 - 5 = 7 - 4$  have the same difference.

**Making 10** using ten frames.

14 - 5



Children to present the ten frame pictorially and discuss what they did to make 10.



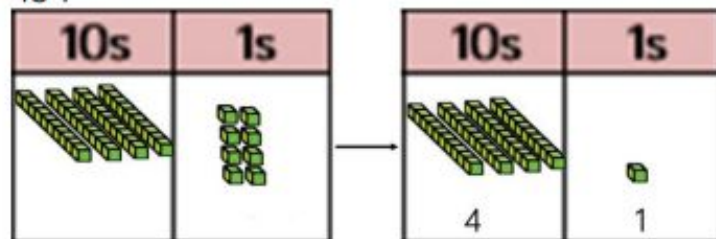
Children to show how they can make 10 by partitioning the subtrahend.

$$\begin{array}{r} 14 - 5 = 9 \\ \swarrow \quad \searrow \\ 4 \quad \quad 1 \end{array}$$

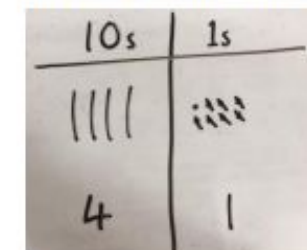
$$\begin{array}{l} 14 - 4 = 10 \\ 10 - 1 = 9 \end{array}$$

**Column method** using base 10.

48-7



Children to represent the base 10 pictorially.



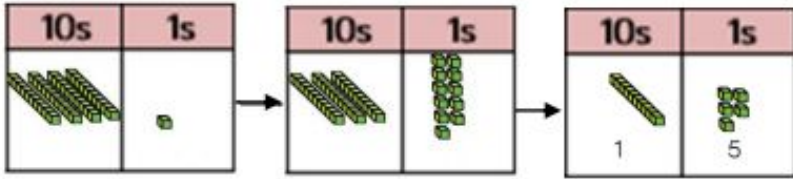
Column method or children could count back 7.

	4	8
-		7
	4	1

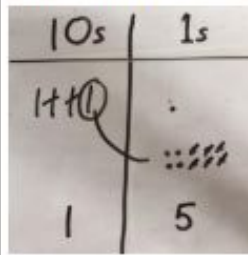


**Column method** using base 10 and having to exchange.

41 - 26



Represent the base 10 pictorially, remembering to show the exchange.

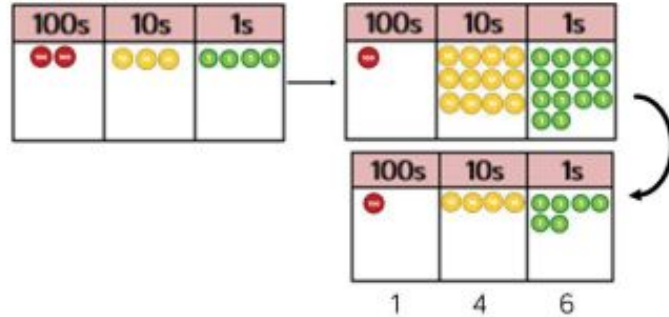


Formal column method. Children must understand that when they have exchanged the 10 they still have 41 because  $41 = 30 + 11$ .

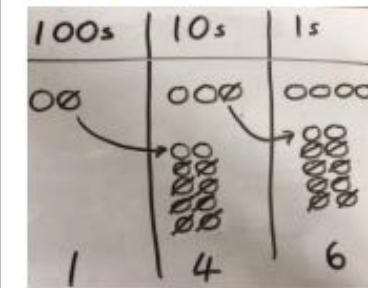
$$\begin{array}{r} 3 \cancel{4} 1 \\ - 26 \\ \hline 15 \end{array}$$

**Column method** using place value counters.

234 - 88



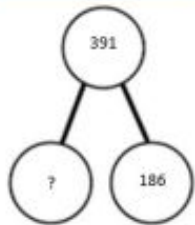
Represent the place value counters pictorially; remembering to show what has been exchanged.



Formal column method. Children must understand what has happened when they have crossed out digits.

$$\begin{array}{r} 2 \cancel{3} 4 \\ - 88 \\ \hline 146 \end{array}$$

## Conceptual variation; different ways to ask children to solve $391 - 186$



391	
186	?

Raj spent £391, Timmy spent £186.  
How much more did Raj spend?

Calculate the difference between 391 and 186.

$$\boxed{\phantom{000}} = 391 - 186$$

391

-186

What is 186 less than 391?

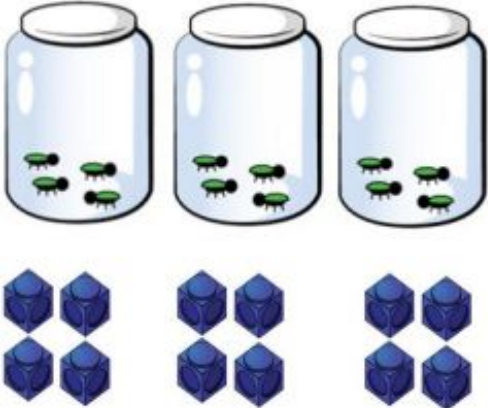
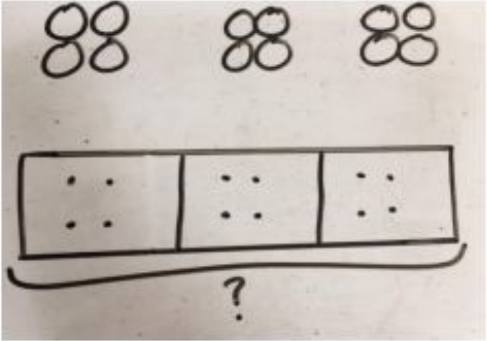
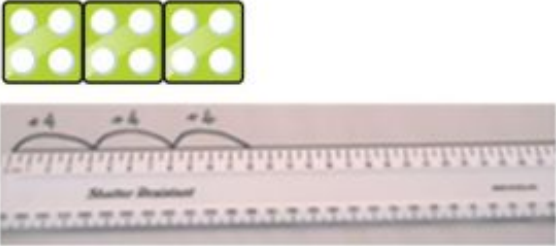
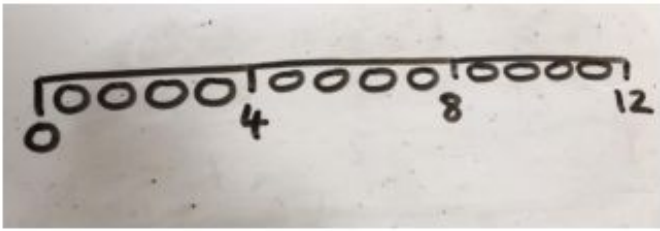
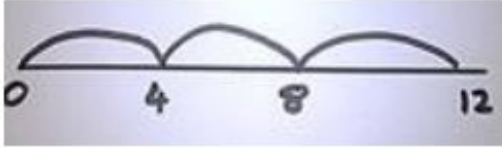
Missing digit calculations

$$\begin{array}{r} 39\boxed{\phantom{0}} \\ - \boxed{\phantom{0}}\boxed{\phantom{0}}6 \\ \hline \boxed{\phantom{0}}05 \end{array}$$



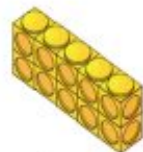
# Calculation policy: Multiplication

Key language: double, times, multiplied by, the product of, groups of, lots of, equal groups.

Concrete	Pictorial	Abstract
<p><b>Repeated grouping/repeated addition</b>  <math>3 \times 4</math>  <math>4 + 4 + 4</math>                      There are 3 equal groups, with 4 in each group.</p> 	<p>Children to represent the practical resources in a picture and use a bar model.</p> 	<p><math>3 \times 4 = 12</math>  <math>4 + 4 + 4 = 12</math></p>
<p><b>Number lines to show repeated groups-</b>  <math>3 \times 4</math></p>  <p>Cuisenaire rods can be used too.</p>	<p>Represent this pictorially alongside a number line e.g.:</p> 	<p>Abstract number line showing three jumps of four.</p> <p><math>3 \times 4 = 12</math></p> 

**Use arrays to illustrate commutativity** counters and other objects can also be used.

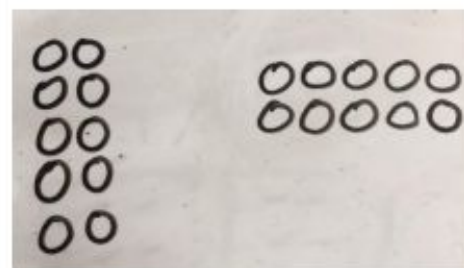
$$2 \times 5 = 5 \times 2$$



2 lots of 5

5 lots of 2

Children to represent the arrays pictorially.



Children to be able to use an array to write a range of calculations e.g.

$$10 = 2 \times 5$$

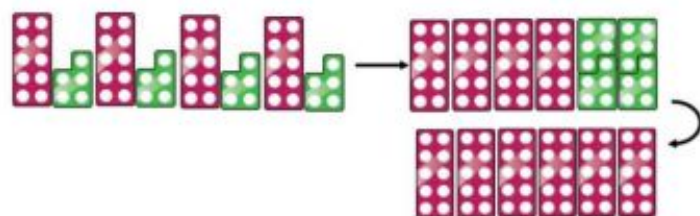
$$5 \times 2 = 10$$

$$2 + 2 + 2 + 2 + 2 = 10$$

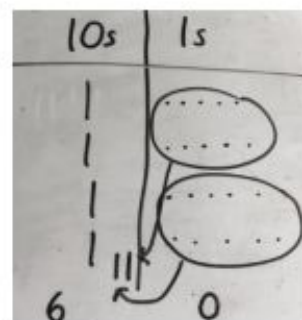
$$10 = 5 + 5$$

**Partition to multiply** using Numicon, base 10 or Cuisenaire rods.

$$4 \times 15$$



Children to represent the concrete manipulatives pictorially.



Children to be encouraged to show the steps they have taken.

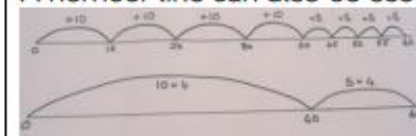
$$\begin{array}{r} 4 \times 15 \\ \swarrow \searrow \\ 10 \quad 5 \end{array}$$

$$10 \times 4 = 40$$

$$5 \times 4 = 20$$

$$40 + 20 = 60$$

A number line can also be used



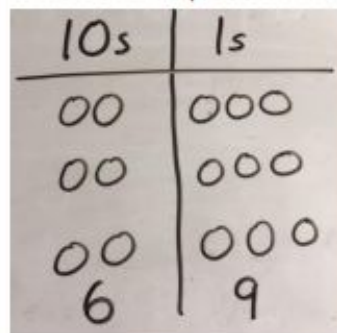
**Formal column method** with place value counters (base 10 can also be used.)  $3 \times 23$

10s	1s

6

9

Children to represent the counters pictorially.



Children to record what it is they are doing to show understanding.

$$3 \times 23$$

$$3 \times 20 = 60$$




$$3 \times 3 = 9$$

$$60 + 9 = 69$$

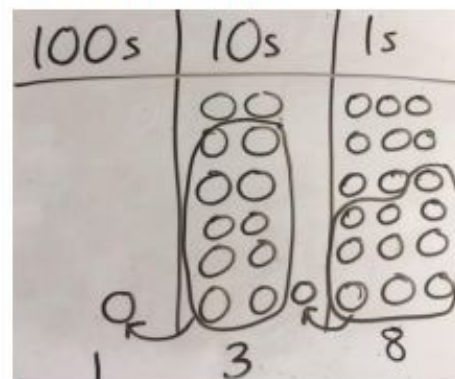
$$\begin{array}{r} 23 \\ \times 3 \\ \hline 69 \end{array}$$

**Formal column method** with place value counters.

100s	10s	1s
		

100s	10s	1s
		

Children to represent the counters/base 10, pictorially e.g. the image below.



Formal written method

$$6 \times 23 =$$

$$\begin{array}{r} 23 \\ \times 6 \\ \hline 138 \\ 11 \end{array}$$

When children start to multiply  $3d \times 3d$  and  $4d \times 2d$  etc., they should be confident with the abstract:

To get 744 children have solved  $6 \times 124$ .

To get 2480 they have solved  $20 \times 124$ .

$$\begin{array}{r} 124 \\ \times 26 \\ \hline 744 \\ 2480 \\ \hline 3224 \end{array}$$

Answer: 3224

## Conceptual variation; different ways to ask children to solve $6 \times 23$

23	23	23	23	23	23
----	----	----	----	----	----

?

Mai had to swim 23 lengths, 6 times a week.  
How many lengths did she swim in one week?

With the counters, prove that  $6 \times 23 = 138$


Find the product of 6 and 23

$$6 \times 23 =$$

$$\boxed{\phantom{00}} = 6 \times 23$$

$$\begin{array}{r} 6 \quad 23 \\ \times 23 \\ \hline \end{array} \quad \begin{array}{r} 6 \\ \times 6 \\ \hline \end{array}$$

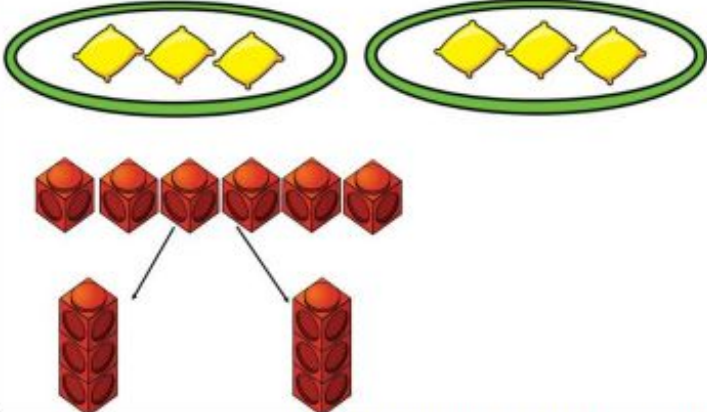
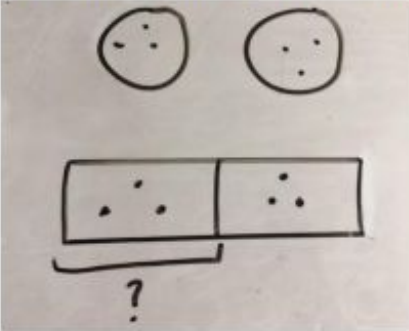

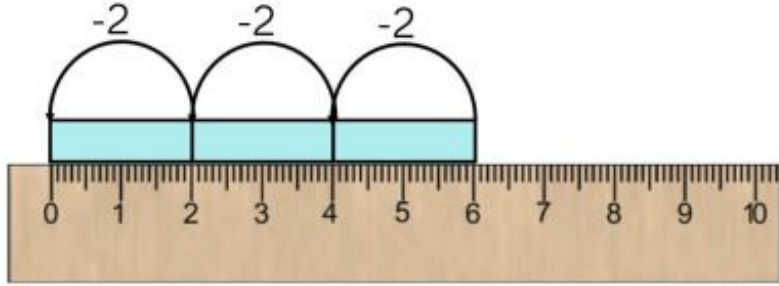
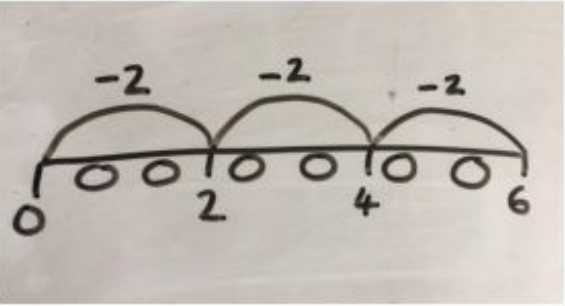
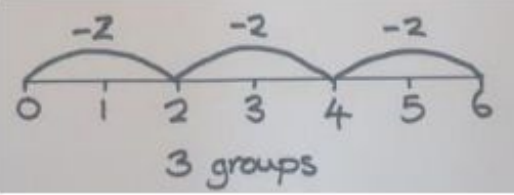
What is the calculation?  
What is the product?

100s	10s	1s
		



# Calculation policy: Division

Key language: share, group, divide, divided by, half.

Concrete	Pictorial	Abstract
<p><b>Sharing</b> using a range of objects.  <math>6 \div 2</math></p>  <p>The image shows two green ovals, each containing three yellow diamonds. Below them, six red Cuisenaire rods are arranged in a row. Two arrows point from the first and fourth rods to two separate vertical stacks of three rods each, illustrating the division of 6 into 2 groups of 3.</p>	<p>Represent the sharing pictorially.</p>  <p>The image shows two hand-drawn circles, each containing three dots. Below them, a rectangle is divided into two equal halves, each containing three dots. A bracket under the first half is labeled with a question mark, indicating the task of representing the division pictorially.</p>	<p><math>6 \div 2 = 3</math></p>  <p>The image shows a simple division problem: 6 divided by 2 equals 3. Below the equation, a table with two columns and one row is shown, with the number 3 in each column.</p> <p>Children should also be encouraged to use their 2 times tables facts.</p>
<p><b>Repeated subtraction</b> using Cuisenaire rods above a ruler.  <math>6 \div 2</math></p>  <p>The image shows a ruler with markings from 0 to 10. Three blue Cuisenaire rods are placed end-to-end on the ruler, starting from 0 and ending at 6. Above each rod, the number -2 is written, indicating the subtraction of 2 from the total. Below the ruler, the text '3 groups of 2' is written.</p>	<p>Children to represent repeated subtraction pictorially.</p>  <p>The image shows a hand-drawn number line from 0 to 6. Three arcs are drawn above the line, each starting at 0, 2, and 4, and ending at 2, 4, and 6 respectively. Each arc is labeled with -2. Below the line, the numbers 0, 2, 4, and 6 are marked, and the text '3 groups' is written below the line.</p>	<p>Abstract number line to represent the equal groups that have been subtracted.</p>  <p>The image shows a hand-drawn number line from 0 to 6. Three arcs are drawn above the line, each starting at 0, 2, and 4, and ending at 2, 4, and 6 respectively. Each arc is labeled with -2. Below the line, the numbers 0, 1, 2, 3, 4, 5, and 6 are marked, and the text '3 groups' is written below the line.</p>

**2d + 1d with remainders** using lollipop sticks. Cuisenaire rods, above a ruler can also be used.

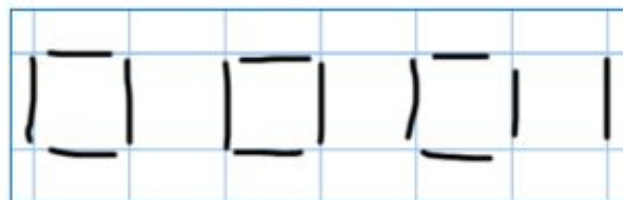
$$13 \div 4$$

Use of lollipop sticks to form wholes- squares are made because we are dividing by 4.



There are 3 whole squares, with 1 left over.

Children to represent the lollipop sticks pictorially.

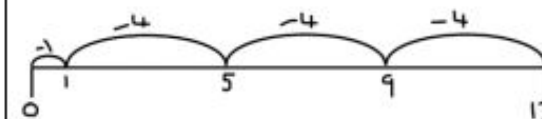


There are 3 whole squares, with 1 left over.

$$13 \div 4 = 3 \text{ remainder } 1$$

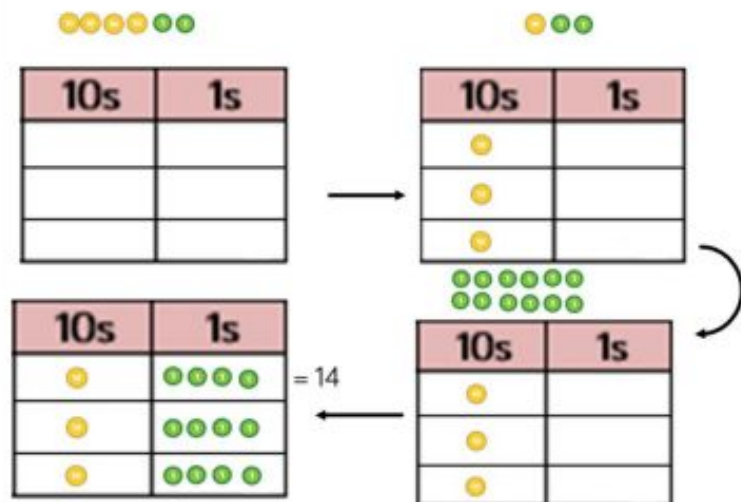
Children should be encouraged to use their times table facts; they could also represent repeated addition on a number line.

'3 groups of 4, with 1 left over'

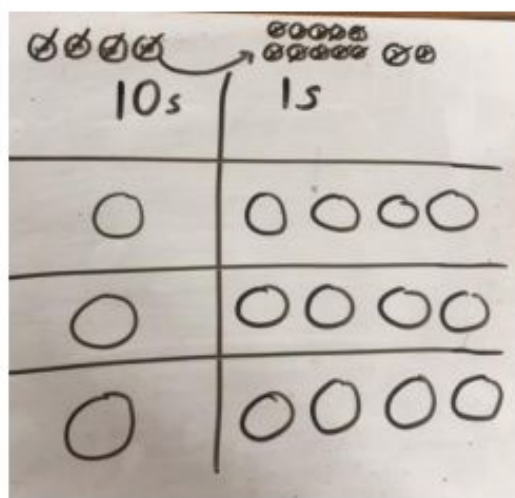


**Sharing using place value counters.**

$$42 \div 3 = 14$$



Children to represent the place value counters pictorially.



Children to be able to make sense of the place value counters and write calculations to show the process.

$$42 \div 3$$

$$42 = 30 + 12$$

$$30 \div 3 = 10$$

$$12 \div 3 = 4$$

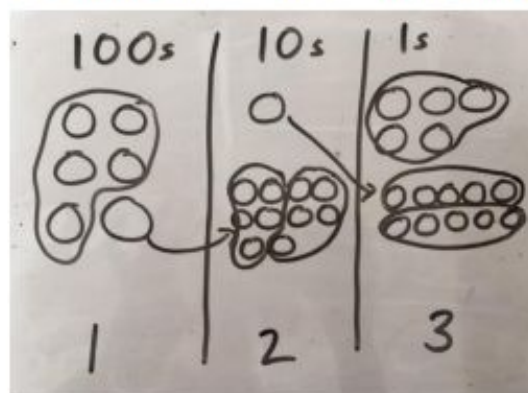
$$10 + 4 = 14$$

**Short division** using place value counters to group.  
 $615 \div 5$

100s	10s	1s
1	2	3

1. Make 615 with place value counters.
2. How many groups of 5 hundreds can you make with 6 hundred counters?
3. Exchange 1 hundred for 10 tens.
4. How many groups of 5 tens can you make with 11 ten counters?
5. Exchange 1 ten for 10 ones.
6. How many groups of 5 ones can you make with 15 ones?

Represent the place value counters pictorially.



Children to the calculation using the short division scaffold.

$$\begin{array}{r} 123 \\ 5 \overline{) 615} \end{array}$$

**Long division** using place value counters  
 $2544 \div 12$

1000s	100s	10s	1s

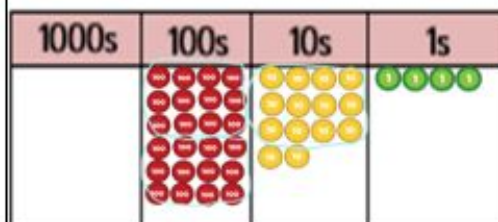
We can't group 2 thousands into groups of 12 so will exchange them.

1000s	100s	10s	1s

We can group 24 hundreds into groups of 12 which leaves with 1 hundred.

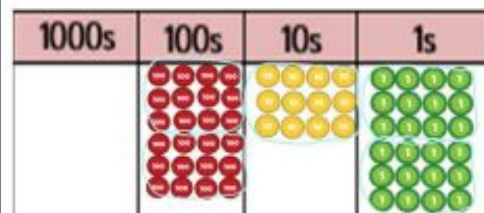
$$\begin{array}{r} 02 \\ 12 \overline{) 2544} \\ \underline{24} \\ 1 \end{array}$$





After exchanging the hundred, we have 14 tens. We can group 12 tens into a group of 12, which leaves 2 tens.

$$\begin{array}{r} 021 \\ 12 \overline{) 2544} \\ \underline{24} \phantom{0} \\ 14 \phantom{0} \\ \underline{12} \phantom{0} \\ 2 \phantom{0} \end{array}$$

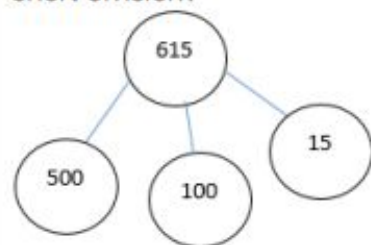


After exchanging the 2 tens, we have 24 ones. We can group 24 ones into 2 group of 12, which leaves no remainder.

$$\begin{array}{r} 0212 \\ 12 \overline{) 2544} \\ \underline{24} \phantom{0} \\ 14 \phantom{0} \\ \underline{12} \phantom{0} \\ 24 \phantom{0} \\ \underline{24} \phantom{0} \\ 0 \end{array}$$

## Conceptual variation; different ways to ask children to solve $615 \div 5$

Using the part whole model below, how can you divide 615 by 5 without using short division?



I have £615 and share it equally between 5 bank accounts. How much will be in each account?

615 pupils need to be put into 5 groups. How many will be in each group?

$$5 \overline{) 615}$$

$$615 \div 5 =$$

$$\square = 615 \div 5$$

What is the calculation?  
What is the answer?

